

Low-scale seesaw and dark matter

M. Fabbrichesi[‡] and S. Petcov^{†‡◦}

[‡]*INFN, Sezione di Trieste*

[†]*SISSA, via Bonomea 265, 34136 Trieste, Italy and*

[◦]*Kavli IPMU, University of Tokyo, Japan*

(Dated: April 16, 2013)

We discuss how two birds—the little hierarchy problem of low-scale type-I seesaw models and the search for a viable dark matter candidate—are (proverbially) killed by one stone: a new inert scalar state

PACS numbers: 14.60.Pq, 14.80.Bn, 95.35.+d

Together with the presence of dark matter (DM), neutrino oscillations—and the small neutrino mass entailed by them—are the only physics beyond the standard model (SM) experimentally confirmed.

The most attractive model to account for the smallness of the neutrino masses is the seesaw mechanism [1]. This mechanism requires right-handed (RH) neutrinos whose masses can be taken at the GUT scale or, in low-scale scenarios, at lower energies if the Yukawa couplings are taken proportionally smaller, for instance, of the order of those of the charged leptons.

The inclusion of these new states within the SM induces a finite renormalization that tends to pull the Higgs boson mass (or, equivalently, the electroweak (EW) scale) toward the higher scale. This is not a problem if the new states are themselves at the EW scale and the renormalization is itself of the order of the Higgs boson mass. If instead the new states are at a larger scale, they give rise to a hierarchy problem in which to keep the Higgs boson mass to its values we have to cancel the renormalization to the higher scale.

Rather than accomplishing such a cancellation by a simple redefinition of the bare masses—a procedure that would require a cancellation between UV and IR degrees of freedom which seems artificial even though technically possible—it is more appealing and practical to use the hierarchy problem in a heuristic manner to help us in the definition of whatever model of physics we assume to exist beyond the SM [2].

In this Letter we discuss the case in which the masses of the RH neutrinos are in the range between 1 and 10 TeV. The renormalization effects are in this case dominated by the one-loop order and we have what has been called the little hierarchy problem. To avoid this problem, new states in addition to the RH neutrinos must be included. As a matter of fact, the addition of one new state is enough. We study its properties and to what extent is a viable candidate for DM. This way, two birds (the little hierarchy problem and DM) are killed by one stone (the new state).

To avoid confusion, let us stress that the hierarchy problem is often discussed in terms of the quadratic divergence arising in the mass term of the Higgs boson in a momentum dependent regularization (or, equivalently, in a pole in $d = 2$ dimensions in dimensional regular-

ization). The presence of these divergences makes the Higgs boson mass extremely sensitive to the UV physics and some cancellation must take place either in a natural manner by assuming a symmetry (usually, supersymmetry) or by fine-tuning by imposing the Veltman condition [3]—namely that the new sector couples to the SM Higgs boson just so as to make the quadratic divergences to the SM Higgs boson mass vanish (see [4] for various applications of this idea). This is not the hierarchy problem we discuss in this Letter.

The point of view we follow is that all quadratic divergences are a scheme-dependent artifact (similar to the quadratic divergence arising in QED when we take a momentum dependent regularization which violates gauge symmetry). In the Higgs boson mass case, they arise because of the explicit breaking of scale invariance in momentum dependent regularizations, and should be eliminated by an appropriated counterterm [5] or by not using that particular regularization scheme. The point is that, even without these divergent terms, there are large finite renormalization effects which only depends on integrating out the heavy modes in the low-energy effective theory—the SM in our case. We identify the little hierarchy problem with the presence of these finite terms. These terms are similar to those arising in a supersymmetric theory with soft mass terms where the quadratic divergences are cancelled while, after integrating out the heavy states, there are finite terms whose contribution shifts the values of the Higgs boson mass. This Letter is about these terms in the case of the seesaw mechanism.

We consider a type I seesaw model in which three RH neutrinos N_{aR} are added to the SM as $SU(2)_L$ singlets. The lagrangian of the model is given by the kinetic and Yukawa terms of the SM with the addition of the neutrino Yukawa terms:

$$\mathcal{L} = -y_{a\ell}^\nu \bar{N}_{aR} \tilde{H}^\dagger L_\ell - \frac{1}{2} \bar{N}_{aL}^c M_{Nab} N_{bR} + H.c., \quad (1)$$

where L_ℓ represents the SM left-handed $SU(2)$ doublet $(\nu_\ell, \ell)_L$ and $\ell = e, \mu, \tau$. In eq. (1), the Yukawa term gives rise to the neutrino Dirac mass matrix, $M_D = y v_W$, after the Higgs field $H = (v_W + h)$ takes its vacuum expectation value $v_W = 174$ GeV. The heavy RH neutrinos N_{aR} have a Majorana mass term.

We compute the one-loop finite correction to the Higgs

boson mass using dimensional regularization with renormalization scale μ . The SM particle contributions are negligible. To compute the one-loop renormalization arising from the heavy Majorana neutrinos, we rotate the Yukawa couplings y_{al}^ν into the basis in which the heavy RH neutrino mass matrix M_N is diagonal. In this basis the matrix of neutrino Yukawa couplings takes the following form in the type I seesaw model of interest [6, 7]:

$$\hat{y}_{j\ell}^\nu = M_{N_j}(RV)_{j\ell}^T/v_W, \quad (2)$$

where V is a unitary matrix which diagonalises the RH neutrino Majorana mass matrix, $M_N = V\hat{M}V^T$ with $\hat{M} = \text{diag}(M_1, M_2, M_3)$, M_j being the mass of the heavy neutrino mass-eigenstate N_j , and $R^T \cong M_N^{-1} M_D$ ($|M_D| \ll |M_N|$). As can be shown (see, *e.g.*, [6]), the quantity $(RV)_{\ell j}$ represents the weak charged current and neutral current coupling of the heavy Majorana neutrino N_j to the charged lepton l and the W^\pm -bosons, and to the LH flavor neutrino ν_l and the Z^0 -boson. The matrix $\eta = -0.5(RV)(RV)^\dagger$ describes, in the seesaw model considered, the deviations from unitarity of the Pontecorvo, Maki, Nakagawa, Sakata (PMNS) neutrino mixing matrix U_{PMNS} : $U_{\text{PMNS}} = (1 + \eta)U$, where U is a unitary matrix which diagonalises the Majorana mass matrix of the LH flavor neutrinos, m_ν , generated by the seesaw mechanism.

In the type I seesaw scenario, the elements of the matrix (RV) are bounded by their relation to the elements of the neutrino mass matrix m_ν [6], which all have to be smaller than approximately 1 eV:

$$\left| \sum_k (RV)_{\ell'k}^* M_k (RV)_{k\ell}^\dagger \right| = |(m_\nu)_{\ell'\ell}| \lesssim 1 \text{ eV}. \quad (3)$$

In the traditional seesaw model the Yukawa couplings are taken typically to be of order one and the masses M_{N_j} are very large, close to the GUT scale. The couplings $|(RV)_{\ell k}|$ in this case have to be very small to satisfy eq. (3). In low-scale seesaw models, the heavy Majorana neutrino masses lie at the TeV scale and the couplings $|(RV)_{\ell k}|$ are proportionally larger. In this scenario, $|(RV)_{\ell k}|$ can even be larger if there is partial or complete cancellation between the terms in the sum in the r.h.s. of eq. (3). This possibility can be realized, *e.g.*, in models [8] with two heavy Majorana neutrinos N_1 and N_2 , which have relatively close masses, $M_2 = M_1(1 + z)$, $z \ll 1$, thus forming a pseudo-Dirac state [9], and whose couplings $(RV)_{\ell 1}$ and $(RV)_{\ell 2}$ are related: $(RV)_{\ell 2}\sqrt{M_2} = \pm i (RV)_{\ell 1}\sqrt{M_1}$, $l = e, \mu, \tau$. The indicated conditions can take place, for instance, in theories with an approximately conserved lepton charge (see, *e.g.*, [10]).

In the scenario with two heavy Majorana neutrinos outlined above, the flavor structure of the couplings $(RV)_{\ell j}$, $j = 1, 2$, is completely determined by the requirement of reproducing the neutrino oscillation data and the scheme is characterized by four parameters [8]: M_1 , z , the largest eigenvalue y of the matrix of neutrino

Yukawa couplings (see further) and a CP violation phase. The neutrino oscillation data, the EW precision measurements and the existing limits on the rates of lepton flavor violating (LFV) processes involving the charged leptons (as the $\mu \rightarrow e + \gamma$, $\mu \rightarrow 3e$ decays, *etc.*), imply the following upper bounds on the couplings $|(RV)_{\ell 1}| \cong |(RV)_{\ell 2}|$ (see, *e.g.*, [11, 12] and references quoted therein):

$$|(RV)_{e1}|^2, |(RV)_{\mu 1}|^2, |(RV)_{\tau 1}|^2 \lesssim 10^{-3} \quad (4)$$

where we have quoted a somewhat simplified constraint on the three couplings. The actual upper bounds depend on the flavor index l of the couplings, but the variation with l is not significant and for the purposes of our investigation it can be neglected. We will use the generic bounds given in eq. (4) in our analysis.

In what follows we will neglect for simplicity the splitting between the two heavy Majorana neutrino masses z , i.e., we will set $z = 0$ and will use $M_1 = M_2 \equiv M_N$. The corrections due to $z \neq 0$ are insignificant in the problem of interest. For $z = 0$, the largest eigenvalue y of the matrix of neutrino Yukawa couplings is given by [8]

$$y^2 v_W^2 = 2M_N^2 [|(RV)_{e1}|^2 + |(RV)_{\mu 1}|^2 + |(RV)_{\tau 1}|^2] \quad (5)$$

Taking into account the one-loop contribution, and assuming RH neutrino degeneracy, the Higgs boson mass receives a shift given by

$$\delta\mu_H^2(\mu) = \frac{4y^2}{(4\pi)^2} M_N^2 \left(1 - \log \frac{M_N^2}{\mu^2} \right), \quad (6)$$

being μ the matching scale that in this case we can identify with M_N .

The addition of the RH neutrinos would shift the Higgs boson mass to the new scale unless we balance this new contribution to prevent large one-loop renormalizations. The identification of what states (their masses and couplings to the Higgs boson) must be present for such a balancing act to occur provides the heuristic power of the little hierarchy problem.

While many possible new states can be added to prevent large corrections to the Higgs boson mass, the simplest choice consists in including just an inert scalar state [13, 14], that is, a scalar particle only interacting with the Higgs boson (and gravity)—and therefore transforming as the singlet representation of the EW gauge group $SU(2) \times U(1)$ (and similarly not charged under the color group)—which acquire no vacuum expectation value. Such a choice minimizes unwanted effects on EW radiative corrections and other physics well described by the SM.

If in addition we impose a Z_2 symmetry under which the inert scalar is odd and all the SM fields are even, the new state will couple to the SM Higgs doublet only through quartic interactions in the scalar potential. By construction, as only look for solutions with vanishing vacuum expectation value, the symmetry Z_2 remains unbroken and after EW symmetry breaking the singlet state

can, as we shall discuss, potentially be a viable cold DM candidate.

The scalar potential of the model is given by

$$V(H, S) = \mu_H^2 (H^\dagger H) + \mu_S^2 S^2 + \lambda_1 (H^\dagger H)^2 + \lambda_2 S^4 + \lambda_3 (H^\dagger H) S S. \quad (7)$$

Linear and trilinear terms for S are absent due to the Z_2 symmetry mentioned above.

Taking into account the one-loop contribution induced by the scalar state S , the overall shift to μ_H^2 , taking $M_S < M_N$ and $\mu = M_S$ to minimize the logarithmic contributions to the matching, becomes

$$\delta\mu_H^2(M_S) = \frac{1}{(4\pi)^2} \left[\lambda_3 M_S^2 - 4y^2 M_N^2 \left(1 - \log \frac{M_N^2}{M_S^2} \right) \right], \quad (8)$$

where we have taken y given in eq. (5) for the Yukawa couplings.

We want the correction in eq. (8) to be of the order of the Higgs boson mass itself. For simplicity, we can just impose that $\delta\mu_H^2 = 0$ and obtain

$$\lambda_3 = \frac{4y^2 M_N^2}{M_S^2} \left(1 - \log \frac{M_N^2}{M_S^2} \right). \quad (9)$$

Equation (9) is economical but we must bear in mind that it represents just a special case in which the one-loop renormalization exactly vanishes. More solutions can easily be found for $\delta\mu_H^2 \simeq m_h^2$ but do not change in a significant manner the numerical results.

Because of the extra factor $1/(4\pi)^2$, two-loop corrections become important only if the masses are above 10 TeV. To be safe, we take the matching scale $\mu = M_S$ smaller than 7 TeV.

It has been shown [14] that a single inert singlet that couples with the Higgs boson with a small coupling is a realistic cold weakly interacting DM candidate (WIMP) with a mass below v_W . In our case, the singlet may account for the correct relic density in the opposite regime where its mass is much larger than v_W and its coupling with the Higgs boson relatively large.

In this case, the scattering amplitude is dominated by the point-like $SS \rightarrow hh$ vertex which gives a contribution to the thermally averaged total cross section equal to

$$\langle\sigma v\rangle \simeq \frac{1}{4\pi} \frac{\lambda_3^2}{M_S^2} \sqrt{1 - \frac{m_h^2}{m_S^2}}, \quad (10)$$

where we keep only the s-wave contribution.

To estimate the viability of S as DM candidate, we must compute its relative relic abundance [15]

$$\Omega_S = \frac{M_S n_S(t_0)}{\rho_c} \quad (11)$$

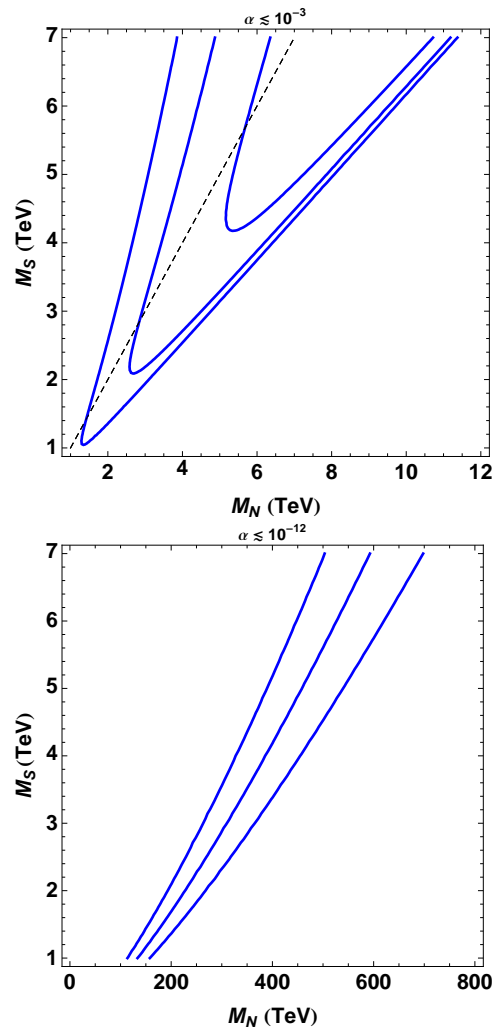


FIG. 1: Contour plot for the WIMP solution: Values of M_S and M_N that are solutions of eq. (16) for two limiting sets of values of the parameter α . On top, (in descending order) $\alpha = \{1, 2, 4\} \times 10^{-4}$, below $\alpha = \{1, 2, 4\} \times 10^{-13}$. Solutions with $m_S < m_N$ are below the dashed line in the figure on top.

where $\rho_c = 1.05 h^2 10^{-5} \text{ GeV/cm}^3$ and the density $n_S(t_0)$ is given by

$$n_S(t_0) = \sqrt{\frac{45}{\pi g_*}} \frac{s_0}{M_{pl} T_f \langle\sigma v\rangle}, \quad (12)$$

where M_{pl} is the Planck mass, T_f is the freeze-out temperature, which for our and similar candidates is approximately given by

$$m_S/T_f \simeq \log \frac{M_S M_{pl} \langle\sigma v\rangle}{240 \sqrt{g_*}} \sim 26, \quad (13)$$

and $s_0 = 2.8 \times 10^3 \text{ cm}^{-3}$ is the entropy density. The constant $g_* = 106.75 + 1$ counts the number of SM degrees of freedom in thermal equilibrium plus the additional degrees of freedom related to the singlet.

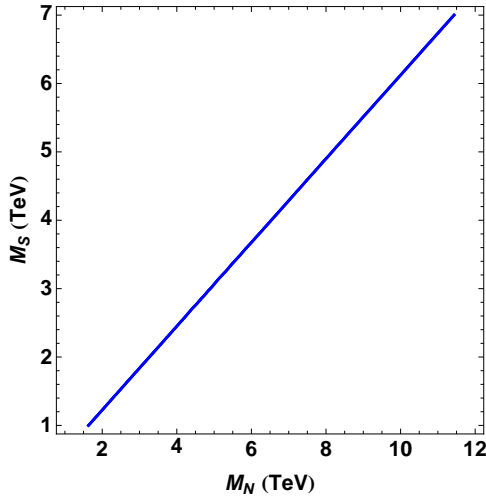


FIG. 2: Contour plot for the FIMP solution: Values of M_S and M_N that are solutions of eq. (9) in the case of $\lambda_3 \simeq 10^{-11}$ and $\alpha \simeq 10^{-12}$.

We therefore obtain

$$\Omega_S h^2 \simeq 8.41 \times 10^{-11} \frac{M_S}{T_f} \sqrt{\frac{45}{\pi g_*}} \frac{\text{GeV}^{-2}}{\langle \sigma v \rangle}, \quad (14)$$

which is sufficiently accurate for our purposes.

Current data fit within the standard cosmological model give a relic abundance with $\Omega_{\text{DM}} h^2 = 0.1187 \pm 0.0017$ [16]. By combining the central value above with eq. (10) and eq. (14), we can write the coupling λ_3 as function of M_S thus obtaining

$$|\lambda_3| \simeq 0.15 \frac{M_S}{\text{TeV}}. \quad (15)$$

This solution gives a DM candidate which can account for 100% of the relic density and with a cross section of a few pb which makes it weakly interacting, a WIMP.

The presence of the scalar singlet DM improves the EW vacuum stability with respect to the SM [17]. This is particularly interesting in connection with the presence of the RH neutrinos which, in general, have the opposite effect of reducing the stability region of the Higgs boson potential [18].

Insertion of eq. (15) in eq. (9) gives a relationship between the RH neutrino mass and that of the new scalar if the latter is to be considered a viable candidate for DM:

$$0.15 M_S^3 = 8 \alpha \frac{M_N^4}{v_W^2} \left(1 - \log \frac{M_N^2}{M_S^2} \right) \quad (16)$$

where $\alpha = |(RV)_{e1}|^2 + |(RV)_{\mu 1}|^2 + |(RV)_{\tau 1}|^2$ represents the sum of the squares of the couplings of the RH and LH neutrinos. In eq. (16), all masses must be taken in TeVs.

Possible solutions are shown in Fig. 1. We can see that we can have solutions with $M_S \simeq M_N$ as long as we

take the couplings between LH and RH neutrinos, and therefore α , to be as large as possible within the experimental constraints in eq. (4). This case corresponds to taking the largest Yukawa coupling just at its experimental bound. This is the most interesting range because the RH neutrino masses are still in a range accessible to the experiments (*e.g.*, $\mu \rightarrow e + \gamma$, $\mu \rightarrow 3e$ decays, $\mu^- - e^-$ conversion in nuclei, neutrinoless double β -decay).

On the other hand, if these couplings are taken at their natural values (and no cancellation is assumed in their sum) we can have only solutions where M_S is much smaller than M_N because now the Yukawa couplings are much smaller than 1. In this case, λ_3 becomes negative and one has to check that $\lambda_3 \geq -2\sqrt{\lambda_1 \lambda_2}$ for the stability of the potential. This scenario seems less interesting than the previous one because the RH neutrino masses are several hundreds of TeVs and therefore outside the range of any foreseeable experiment.

It is interesting to notice that there exists another regime in which the inert singlet is a viable DM candidate. When λ_3 is much smaller than 1, thermal equilibrium for the scalar states is never attained and their abundance is so low that they never annihilate among themselves. The usual result does not apply. In this case, the DM candidate is what has been called a feebly interacting massive particle (FIMP). If we do not use eq. (15) and take $\lambda_3 \simeq 10^{-11}$ [19], we can have a DM candidate in which $M_S \simeq M_N$ (see Fig. 2). For these solutions, $\alpha \simeq 10^{-12}$ and the Yukawa couplings become of the order of those of the charged leptons.

Let us briefly comment on the possibility of detecting the inert scalar S in the case in which is a WIMP. The multi TeV range of its mass makes its detection at the LHC very difficult if not impossible. Whereas a detailed discussion of its possible role in the phenomena observed by the current experiments in space (PAMELA, FERMI, AMS2 *etc.*) is beyond the scope of this Letter, nuclear scattering experiments are more promising and easier to quantify. The quartic term proportional to λ_3 in eq. (7) gives rise, after EW symmetry breaking, to the three-field interaction SSh which yields the effective singlet-nucleon vertex $f_N \lambda_3 m_N / m_h^2 SS \bar{\psi}_N \psi_N$, where m_N is the nucleon mass and the factor f_N contains many uncertainties due to the computation of the nuclear matrix elements and it can vary from 0.3 to 0.6 [20]. The (non-relativistic) cross section for the process is given by [21]

$$\sigma_N = f_N^2 m_N^2 \frac{\lambda_3^2}{4\pi} \left(\frac{m_r}{m_S m_h^2} \right)^2, \quad (17)$$

where m_r is the reduced mass for the system which is, to a very good approximation in our case, equal to the nucleon mass m_N . Substituting the values we have found for our model and for m_S of a few TeV, we obtain, depending on the choice of parameters and within the given uncertainties, a cross section σ_N of order 10^{-45}cm^2 , a value within reach of the next generation of experiments [22].

Acknowledgments

This research was supported in part by the World Premier International Research Center Initiative (WPI Ini-

tiative), MEXT, Japan, by the European Union FP7-ITN INVISIBLES (Marie Curie Action, PITAN-GA-2011-289442) and by the INFN program on “Astroparticle Physics” (S.T.P.).

-
- [1] P. Minkowski, Phys. Lett. **B67**, 421 (1977); M. Gell-Mann, P. Ramond and R. Slansky, (1979), Print-80-0576 (CERN); T. Yanagida, (KEK lectures, 1979), ed. Sawada and Sugamoto (KEK, 1979); R. N. Mohapatra and G. Senjanovic, Phys. Rev. Lett. **44**, 91 (1980).
 - [2] F. Bazzocchi and M. Fabbrihesi, Phys. Rev. D **87**, 036001 (2013) [arXiv:1212.5065].
 - [3] M. J. G. Veltman, Acta Phys. Polon. B **12**, 437 (1981); see, also, P. Osland and T. T. Wu, Phys. Lett. B **291**, 315 (1992); E. Ma, Phys. Rev. D **47**, 2143 (1993) [hep-ph/9209221]; G. Ossola and A. Sirlin, Eur. Phys. J. C **31**, 165 (2003) [hep-ph/0305050].
 - [4] A. Kundu and S. Raychaudhuri, Phys. Rev. D **53**, 4042 (1996) [hep-ph/9410291]; N. G. Deshpande, R. J. Johnson and E. Ma, Phys. Lett. B **130**, 61 (1983); F. Bazzocchi, M. Fabbrihesi and P. Ullio, Phys. Rev. D **75**, 056004 (2007) [hep-ph/0612280]; B. Grzadkowski and J. Wudka, Phys. Rev. Lett. **103**, 091802 (2009) [arXiv:0902.0628]; A. Drozd, B. Grzadkowski and J. Wudka, JHEP **1204**, 006 (2012) [arXiv:1112.2582]; F. Bazzocchi and M. Fabbrihesi, Eur. Phys. J. C **73**, 2303 (2013) [arXiv:1207.0951].
 - [5] W. A. Bardeen, FERMILAB-CONF-95-391-T; K. A. Meissner and H. Nicolai, Phys. Lett. B **660**, 260 (2008) [arXiv:0710.2840]; M. Shaposhnikov and D. Zenhausern, Phys. Lett. B **671**, 162 (2009) [arXiv:0809.3406].
 - [6] A. Ibarra, E. Molinaro, and S. T. Petcov, JHEP **1009**, 108 (2010) [arXiv:1007.2378].
 - [7] C.G. Cely, A. Ibarra, E. Molinaro, S.T. Petcov, Phys. Lett. B **718** (2013) 957 [arXiv:1208.3654].
 - [8] A. Ibarra, E. Molinaro and S.T. Petcov, Phys. Rev. D **84** (2011) 013005 [arXiv:1103.6217].
 - [9] L. Wolfenstein, Nucl. Phys. B **186** (1981) 147; S.T. Petcov, Phys. Lett. B **110** (1982) 245; C.N. Leung and S.T. Petcov, Phys. Lett. B **125** (1983) 461.
 - [10] M. B. Gavela, T. Hambye, D. Hernandez and P. Hernandez, JHEP **0909** (2009) 038 [arXiv:0906.1461].
 - [11] E. Akhmedov, A. Kartavtsev, M. Lindner, L. Michaels and J. Smirnov, arXiv:1302.1872.
 - [12] D.N. Dinh, A. Ibarra, E. Molinaro and S.T. Petcov, JHEP **1208** (2012) 125 [arXiv:1205.4671].
 - [13] R. Barbieri, L. J. Hall and V. S. Rychkov, Phys. Rev. D **74**, 015007 (2006) [hep-ph/0603188]; V. Barger, P. Langacker, M. McCaskey, M. J. Ramsey-Musolf and G. Shaughnessy, Phys. Rev. D **77**, 035005 (2008) [arXiv:0706.4311 [hep-ph]].
 - [14] V. Silveira and A. Zee, Phys. Lett. B **161**, 136 (1985); J. McDonald, Phys. Rev. D **50**, 3637 (1994) [hep-ph/0702143]; C. P. Burgess, M. Pospelov and T. ter Veldhuis, Nucl. Phys. B **619**, 709 (2001) [hep-ph/0011335]; R. Dick, R. B. Mann and K. E. Wunderle, Nucl. Phys. B **805**, 207 (2008) [arXiv:0803.1444]; C. E. Yaguna, JCAP **0903**, 003 (2009) [arXiv:0810.4267]; K. Cheung, Y. -L. S. Tsai, P. -Y. Tseng, T. -C. Yuan and A. Zee, JCAP **1210**, 042 (2012) [arXiv:1207.4930 [hep-ph]].
 - [15] M. Srednicki, R. Watkins and K. A. Olive, Nucl. Phys. B **310**, 693 (1988); P. Gondolo and G. Gelmini, Nucl. Phys. B **360**, 145 (1991); M. Cirelli, N. Fornengo and A. Strumia, Nucl. Phys. B **753**, 178 (2006) [hep-ph/0512090]; D.S. Gorbunov and V.A. Rubakov, *Introduction to the theory of the early universe*, World Scientific, Singapore, 2011.
 - [16] P. A. R. Ade *et al.* [Planck Collaboration], arXiv:1303.5076 [astro-ph.CO].
 - [17] M. Gonderinger, Y. Li, H. Patel and M. J. Ramsey-Musolf, JHEP **1001**, 053 (2010) [arXiv:0910.3167 [hep-ph]].
 - [18] J. Elias-Miro, J. R. Espinosa, G. F. Giudice, G. Isidori, A. Riotto and A. Strumia, Phys. Lett. B **709**, 2 (2012) [arXiv:1112.3022 [hep-ph]].
 - [19] C. E. Yaguna, JHEP **1108**, 060 (2011) [arXiv:1105.1654]; and JCAP **1202**, 006 (2012) [arXiv:1111.6831].
 - [20] A. Bottino, *et al.* Astropart. Phys. **13**, 215 (2000) [hep-ph/9909228] and **18**, 205 (2002) [hep-ph/0111229].
 - [21] R. Barbieri, M. Frigeni and G. F. Giudice, Nucl. Phys. B **313**, 725 (1989); J. R. Ellis *et al.*, Phys. Rev. D **71**, 095007 (2005) [hep-ph/0502001].
 - [22] M. Schumann (XENON100 collaboration), J. Phys.: Conf. Ser. **309** (2011) 012011 and <http://dmttools.brown.edu/>.